

## Measures of Dispersion (14)

(2) Discrete Series or Frequency Array and Mean Deviation.

following steps may be noted in the calculation of mean deviation for the discrete series:

- (i) Find out central tendency of the series from which deviation are to be taken.
- (ii) Deviation of different items in the series are taken from central tendency, and sign (+) or (-) of the deviation are ignored. It is expressed as  $(dx)$  or  $(dm)$ .
- (iii) Each deviation value is multiplied by the frequency facing it, and the sum of these multiples is obtained. This is expressed as  $\sum f|d|$ .
- (iv)  $\sum f|d|$  is divided by the sum of  $f$  total frequency, that is  $\sum f$  or  $N$ . The resultant value would be mean deviation.

Thus,

$$M.D_m = \frac{\sum f|d_m|}{N}$$

Illustration

Using median and arithmetic mean respectively, calculate mean deviation and its coefficient from following data.

Size	5	6	7	8	9	10	11	12	13
freq	4	5	6	7	8	9	10	11	12

Sol<sup>n</sup>.

Calculation of Mean deviation from Median.

Size of items ( $x$ )	Frequency ( $f$ )	Cf	$ dm  = x - m$ $m = 10$	Multiple of Deviation as the corresponding frequency $f \cdot  dm $
5	4	4	5	20
6	5	9	4	20
7	6	15	3	18
8	7	22	2	14
9	8	30	1	8
10	9	39	0	0
11	10	49	1	10
12	11	60	2	22
13	12	72	3	36
N = 72				$\Sigma f dm  = 148$

(A) Median = Size of  $\frac{N+1}{2}$ th items.

$$= \frac{72+1}{2} \text{th item} = \frac{73}{2} = 36.5$$

$$= 10$$

(B) Mean deviation from Median.

$$MD_m = \frac{\Sigma f|dm|}{N} = \frac{148}{72} = 2.05$$

Coefficient of Mean Deviation from Median.

$$\frac{MD_m}{M} = \frac{2.05}{10} = 0.205$$

## Calculation of Mean Deviation from Mean

$\bar{x} = 9.83$				
X	f	fx	$d\bar{x}$	$f d\bar{x} $
5	4	20	4.83	19.32
6	5	30	3.83	19.15
7	6	42	2.83	16.98
8	7	56	1.83	12.81
9	8	72	0.83	6.64
10	9	90	0.17	1.53
11	10	110	1.17	11.70
12	11	132	2.17	23.87
13	12	156	3.17	38.04
$\sum fx = 708$ $N = 72$			$\sum f d\bar{x}  = 150.04$	

$$(a) \quad \bar{x} = \frac{\sum fx}{N} = \frac{708}{72} = 9.83 \quad \text{Ans}$$

(b) Mean Deviation from  $\bar{x}$

$$= MD_{\bar{x}} = \frac{\sum f|d\bar{x}|}{N} = \frac{150.04}{72}$$

$$= \frac{2.08}{1} = 2.08 \quad \text{Ans}$$

(c) Coefficient of M.D. from Mean

$$\frac{MD_{\bar{x}}}{\bar{x}} = \frac{2.08}{9.83} = 0.21$$