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Kinetic Theory of gases

Kinetic theory of gases is an early form of statistical mechanics.

This theory was largely developed through the work of Clausius , Maxwell and Boltzmann .

They were by Mayer , vander Waals and others .

In the early stage the theory has been developed entirely from a mathematical stand – point , as there was no experimental evidence of molecular motions

Now it has been verified experimentally .

Fundamental Postulates of kinetic theory of gases :

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Followings are the main assumption :

- (1) A gas is composed of a large number of molecules , which are identical for a given gas .
- (2) There is no force of attraction between the molecules .
- (3) molecules obey Newton's law of motion .
- (4) Molecules are perfectly elastic rigid solid spheres , so that there is no loss of energy in a collision .

(5) Between two collisions the molecules move with different velocity in different direction . During the collision they travel an independent path , this path is called free path and average of whole free path is called mean free path . This path is in the order of 10^{-7} meter . The time taken for this mean free path is nearly 10^{-9} sec

(6) The molecules are mere points i.e. dimensions of molecules are negligible .

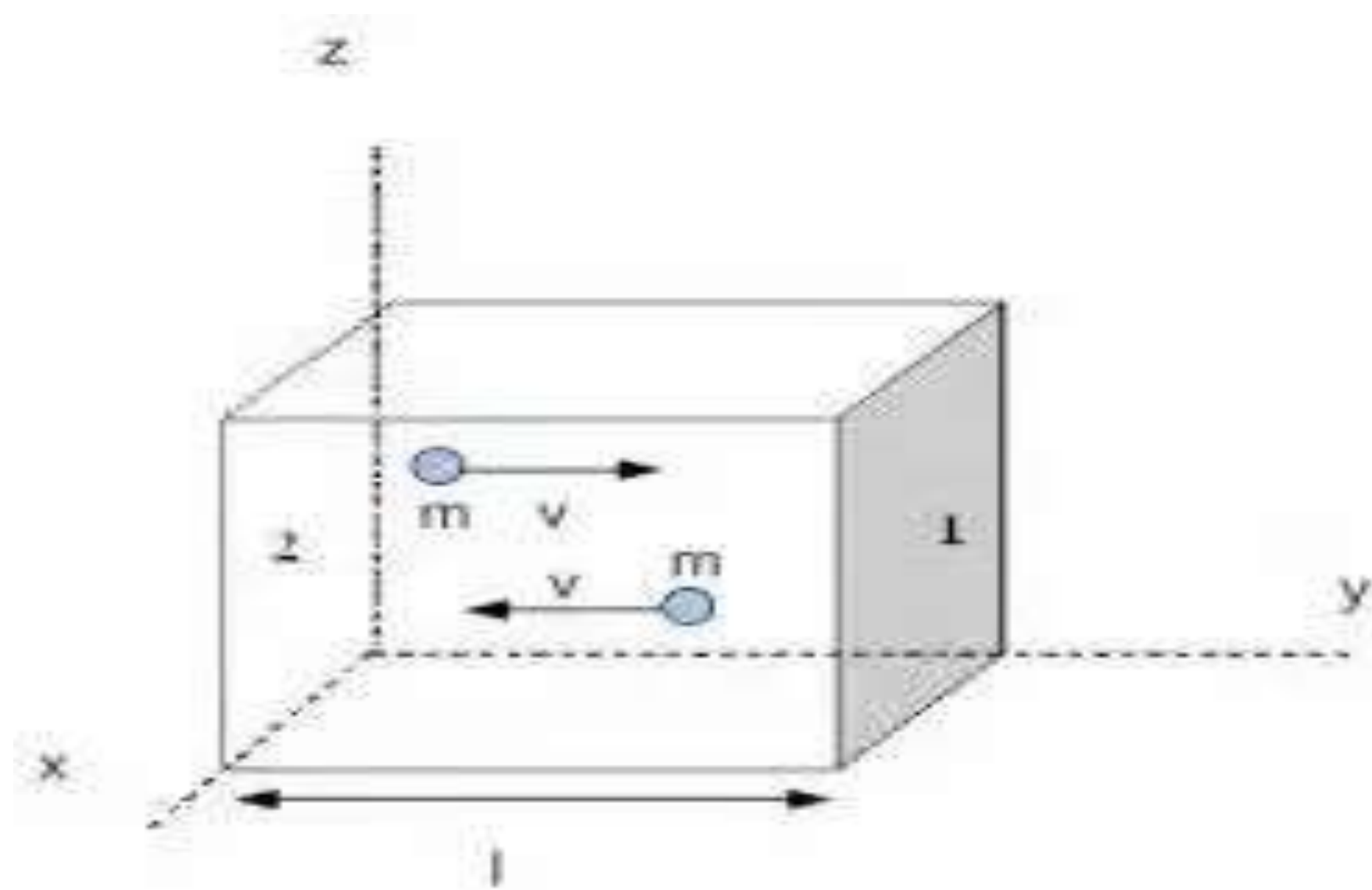
(7) The collisions between molecules and with walls are perfectly elastic so that there is no loss of energy during the collision .

(8) Since the molecules are perfectly elastic so these molecules return back with the same momentum as it was strike upon it .

(9) The pressure of the gas in all directions is the same .

Expression of a perfect gas :

Let us consider a vessel of the shape of a cube . If this vessel be filled up with a gas and each side of the cube measures l . consider a molecule whose velocity in any direction is c their components are along X , Y and Z direction is supposed to be u , v and w respectively , such that



$$c^2 = u^2 + v^2 + w^2$$

If u_1 be the velocity of the first molecule along X – direction, the molecule strike with the momentum mu_1 after collision the molecule returns back with same momentum mu_1 .

$$\text{The change in momentum} = mu_1 - (-mu_1) = 2mu_1 \quad (1)$$

After this the molecule collides with the wall and returns and again collides with the wall .

Thus the molecule successively collides with the wall after travelling a distance $= 2l$.

The molecule takes a time $2l/ u_1$ second .

$$\begin{aligned}\text{Therefore rate of change of momentum} &= 2mu_1 / 2l/u_1 \\ &= 2mu_1 \times u_1 / 2l \\ &= mu_1^2 / l\end{aligned}\tag{2}$$

According to Newton's second law of motion the rate of change in momentum is directly proportional to force .

$$\text{Force} = mu_1^2 / l$$

$$\text{Pressure} = mu_1^2 / l^3 \quad (3)$$

If the cubical vessel contains n molecules then pressure exerted on the wall due to all the molecules is

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$$\begin{aligned} P_x &= mu_1^2 / l^3 + m u_2^2 / l^3 + \dots + mu_n^2 / l^3 \\ &= m/l^3 (u_1^2 + u_2^2 + \dots + u_n^2) \\ &= m/V(u_1^2 + u_2^2 + \dots + u_n^2) \end{aligned} \quad (4)$$

Where $l^3 = V$ Volume of the vessel .

Similarly Pressure along Y axis

$$P_Y = m/V (v_1^2 + v_2^2 + v_3^2 + \dots + v_n^2) \quad (5)$$

Along Z – axis Pressure = $P_Z = m/V(w_1^2 + w_2^2 + \dots + w_n^2)$
(6)

Since the pressure of gas is the same in all directions

$$P = P_X + P_Y + P_Z / 3$$

$$P = m / 3V [(u_1^2 + v_1^2 + w_1^2) + (u_2^2 + v_2^2 + w_2^2) + \dots + (u_n^2 + v_n^2 + w_n^2)]$$

$$P = m / 3V (c_1^2 + c_2^2 + \dots + c_n^2) = mn / 3V (c_1^2 + c_2^2 + \dots + c_n^2) / n$$

$$= MC^2 / 3V \quad (7)$$

$$P = MC^2 / 3V \quad (8)$$

Where $M = mn$ (Total mass of the gas)

and $C^2 = c_1^2 + c_2^2 + c_3^2 + \dots + c_n^2 / n$

C^2 is called mean square velocity and c is called root mean square velocity

Since , density of the gas $\rho = M/V$

Therefore ,Pressure $P = 1/3 \rho C^2$

RMS velocity : $C = \sqrt{3P/\rho}$ (9)

For air , $P = 1.013 \times 10^5 \text{ N/m}^2$ and $\rho = 1.293 \text{ kg /m}^3$

Hence RMS velocity of air $C = 484.8 \text{ m/s}$