

* de-Broglie wave associated with Bohr-orbit in H-atom

In Bohr's theory, electron is treated as a particle, but de-Broglie's theory suggested that matter and therefore, electron also, has a dual character, both as material particle and as a wave. He derived an expression for calculating the wave length λ of a particle of mass m moving with velocity v . A/c to which -

$$\lambda = \frac{h}{mv} \quad \text{--- (1)}$$

A/c to Einstein's mass-energy relationship -

$$E = mc^2 \quad \text{--- (2)}$$

and A/c to Planck's eqs -

$$E = h\nu = \frac{hc}{\lambda} \quad \text{--- (3)}$$

on equating eqs - (2) & (3)

$$\frac{hc}{\lambda} = mc^2$$

$$\therefore \lambda = \frac{h}{mc}$$

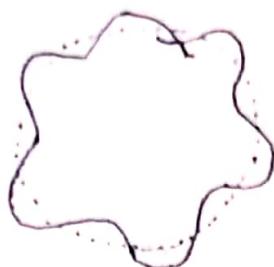
on replacing c by v we have -

$$\lambda = \frac{h}{mv} = \frac{h}{P}$$

Where, P is the momentum of the particle.

* Bohr's angular momentum from de-Broglie's Eq-

Let us consider an electron moving in a circular orbit of radius 'r' around a nucleus. The wave train would be as shown as -



If the wave is to remain continually in phase, the circumference of the circular orbit must be an integral multiple of wave length ' λ '. i.e.

$$2\pi r = n\lambda = \frac{nh}{mv} = \frac{nh}{p}$$

Thus, the angular momentum -

$$L = mvr = \frac{nh}{2\pi}$$

Thus an electron can move only in those orbit for which the angular momentum is an integral multiple of $h/2\pi$.

It is the reason that electrons are allowed to move only in certain fixed orbit.

The angular momentum of electrons in atoms is quantised. for $n = 1, 2, 3, \dots$ the angular momentum will be -

$$\frac{h}{2\pi}, \frac{h}{\pi}, \frac{3h}{2\pi}, \dots \text{. It can have only definite values.}$$