

\* Success of Bohr's atomic model :-

(1) Radius of an atom (Calculation of radius)

Radius may be calculated by following eqs -

$$r_n = \frac{n^2 h^2}{4\pi^2 m e^2 Z} \quad \text{--- (1)}$$

where,  $n$  = no. of orbit

$h$  = plank's constant =  $6.626 \times 10^{-34}$  J sec.

$$\pi = 22/7 = 3.414$$

$m$  = mass of an electron =  $9.1 \times 10^{-31}$  kg

$e$  = charge of an electron =  $1.602 \times 10^{-19}$  C

$Z$  = atomic no.

on putting all these values in eqs - (1), we get.

$$r_n = 0.529 \text{ \AA} \times \frac{h^2}{Z}$$

for H-atoms. —  $n=1, Z=1$

$$r_H = 0.529 \text{ \AA}$$

called Bohr's radius for H-atoms.

for H like species. —

|                    |                       |
|--------------------|-----------------------|
| $\text{He}^+$ ion, | $\text{Li}^{++}$ ion, |
| $n=1, 2, 3, \dots$ | $n=1, 2, 3, \dots$    |
| $Z=2$              | $Z=3$ .               |

## (2). Calculation of Energy :-

The energy of the electron may be calculated from the following formula -

$$E_n = -\frac{2\pi^2 m e^4 z^2}{n^2 h^2} \quad \text{--- (1)}$$

where,  $m$  = mass of an electron =  $9.1 \times 10^{-31}$  kg

$$\pi = 22/7 = 3.14$$

$e$  = charge of an electron =  $1.602 \times 10^{-19}$  C

$z$  = atomic no.

$n$  = orbit no. = 1, 2, 3, ...

$h$  = Planck's constant =  $6.626 \times 10^{-34}$  J sec

Putting all these values in eqs - (1) we get -

$$E_n = -13.6 \times \frac{z^2}{n^2} \text{ eV/atom.} \quad \text{--- (2)}$$

Since,  $1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$

$$E_n = -13.6 \times \frac{z^2}{n^2} \times 1.602 \times 10^{-19} \text{ J/atom.}$$

$$E_n = -21.78 \times \frac{z^2}{n^2} \times 10^{-19} \text{ J/atom}$$

$$E_n = -2.18 \times 10^{-18} \text{ J/atom} \times \frac{z^2}{n^2} \quad \text{--- (3)}$$

$$\text{or } E_n = -2.18 \times 10^{-18} \times 6.022 \times 10^{23} \text{ J/mole} \times \frac{z^2}{n^2}$$

$$E_n = -13.12 \times 10^5 \text{ J/mole} \times \frac{z^2}{n^2}$$

$$\text{or } E_n = -1312 \text{ kJ/mole} \times \frac{Z^2}{n^2} \quad \text{--- (4)}$$

for H-atom

$$n=1, Z=1.$$

$$E_H = -13.6 \text{ eV/atom.}$$

for H-like species -

|                    |                    |
|--------------------|--------------------|
| $\text{He}^+$      | $\text{Li}^{++}$   |
| $n=1, 2, 3, \dots$ | $n=1, 2, 3, \dots$ |
| $Z=2$              | $Z=3$              |

### (3) Calculation of Velocity of an electron :-

Velocity of an electron is calculated by the formula -

$$v_n = \frac{2\pi e^2 Z}{nh} \text{ m sec}^{-1}. \quad \text{--- (1)}$$

$$\text{where, } \pi = 22/7 = 3.414$$

$$e = \text{charge of an electron} = 1.602 \times 10^{-19} \text{ C}$$

$$Z = \text{atomic no.}$$

$$n = \text{orbit no.}$$

$$h = \text{planck's constant} = 6.626 \times 10^{-34} \text{ J sec.}$$

Putting all these values in eqs - (1), we get -

$$v_n = 2.19 \times 10^6 \times \frac{Z}{n} \text{ m sec}^{-1}.$$

$$v_n = 2.19 \times 10^8 \times \frac{Z}{n} \text{ cm sec}^{-1}.$$