

(1)

* Success of Bohr's atomic model :-

(1) Radius of an atom (Calculation of radius)

Radius may be calculated by following eqs -

$$r_n = \frac{n^2 h^2}{4\pi^2 m e^2 Z} \quad \text{--- (1)}$$

Where, n = no. of orbit

h = plank's constant = 6.626×10^{-34} J sec.

$$\pi = \frac{22}{7} = 3.14$$

m = mass of an electron = 9.1×10^{-31} kg

e = charge of an electron = 1.602×10^{-19} C

Z = atomic no.

on putting all these values in eqs --- (1), we get.

$$r_n = 0.529 \text{ \AA} \times \frac{n^2}{Z}$$

for H-atom. - $n=1, Z=1$

$$r_H = 0.529 \text{ \AA}$$

called Bohr's radius for H-atom.

for H like species. -

He ⁺ ion,	Li ⁺⁺ ion,
$n=1,2,3, \dots$	$n=1,2,3, \dots$
$Z=2$	$Z=3$

(2). Calculation of Energy :-

The energy of the electron may be calculated from the following formula -

$$E_n = - \frac{2\pi^2 m e^4 Z^2}{n^2 h^2} \quad \text{--- (1)}$$

Where, m = mass of an electron = 9.1×10^{-31} kg

$$\pi = \frac{22}{7} = 3.14$$

e = charge of an electron = 1.602×10^{-19} C

Z = atomic no.

n = orbit no. = 1, 2, 3, ...

h = Planck's constant = 6.626×10^{-34} Jsec

Putting all these values in eqs --- (1) we get -

$$E_n = -13.6 \times \frac{Z^2}{n^2} \text{ eV/atom.} \quad \text{--- (2)}$$

Since, $1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$

$$E_n = -13.6 \times \frac{Z^2}{n^2} \times 1.602 \times 10^{-19} \text{ J/atom.}$$

$$E_n = -21.78 \times \frac{Z^2}{n^2} \times 10^{-19} \text{ J/atom}$$

$$E_n = -2.18 \times 10^{-18} \text{ J/atom} \times \frac{Z^2}{n^2} \quad \text{--- (3)}$$

$$\approx E_n = -2.18 \times 10^{-18} \times 6.022 \times 10^{23} \text{ J/mole} \times \frac{Z^2}{n^2}$$

$$E_n = -13.12 \times 10^5 \text{ J/mole} \times \frac{Z^2}{n^2}$$

$$E_n = -1312 \text{ kJ/mole} \times \frac{Z^2}{n^2} \quad \text{--- (4)}$$

for H-atom

$$n=1, Z=1.$$

$$E_H = -13.6 \text{ eV/atom.}$$

for H-like species-

He^+	{	Li^{++}
$n=1,2,3, \dots$		$n=1,2,3, \dots$
$Z=2$		$Z=3$

(3) calculation of velocity of an electron :-

Velocity of an electron is calculated by the formula -

$$V_n = \frac{2\pi e^2 Z}{nh} \text{ m sec}^{-1} \quad \text{--- (1)}$$

Where, $\pi = 22/7 = 3.14$

$e = \text{charge of an electron} = 1.602 \times 10^{-19} \text{ C}$

$Z = \text{atomic no.}$

$n = \text{orbit no.}$

$h = \text{planck's constant} = 6.626 \times 10^{-34} \text{ J sec.}$

Putting all these values in eqⁿ --- (1), we get -

$$V_n = 2.19 \times 10^6 \times \frac{Z}{n} \text{ m sec}^{-1},$$

$$V_n = 2.19 \times 10^8 \times \frac{Z}{n} \text{ cm sec}^{-1},$$