Matrices

Simultaneous Equation

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☐ Solve for

$$2x + 3y = 7$$

$$4x + 2y = 10$$

Solution:

Putting the above equation in matrix form;

$$\begin{bmatrix} 2 & 3 \\ 4 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 7 \\ 10 \end{bmatrix}$$

$$A \quad X \quad K$$

$$\square X = A^{-1}K$$

$$|A| = \begin{vmatrix} 2 & 3 \\ 4 & 2 \end{vmatrix} = 4 - 12 = -8$$

Cofactor of
$$2 = 2$$
; Cofactor of $3 = -4$

Cofactor of
$$4 = -3$$
; Cofactor of $2 = 2$

$$Adj A = \begin{bmatrix} 2 & -3 \\ -4 & 2 \end{bmatrix}$$

$$A^{-1} = \frac{1}{-8} \times \begin{bmatrix} 2 & -3 \\ -4 & 2 \end{bmatrix} = \begin{bmatrix} -2/8 & 3/8 \\ 4/8 & -2/8 \end{bmatrix}$$

$$\therefore X = A^{-1}K$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -2/8 & 3/8 \\ 4/8 & -2/8 \end{bmatrix} \times \begin{bmatrix} 7 \\ 10 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} \frac{-14}{8} + \frac{30}{8} \\ \frac{28}{8} - \frac{20}{8} \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} \frac{16}{8} \\ \frac{8}{8} \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \end{bmatrix}$$

 $\therefore x = 2 \ and \ y = 1 \ Answer$

THANK YOU