

- Transpose of a Matrix: A matrix obtained by interchanging rows and columns. It is denoted by A' or A^T .
- For example: if matrix A is

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}, \text{ then transpose of matrix would be}$$
$$A' = \begin{bmatrix} a_{11} & a_{21} & a_{31} \\ a_{12} & a_{22} & a_{32} \\ a_{13} & a_{23} & a_{33} \end{bmatrix}$$

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- Similarly,
- *if*, $A = [x_1 \ x_2 \ x_3]$, then

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$$A' = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

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• Example:

• *if*,
$$A = \begin{vmatrix} 2 & 3 & 4 \\ 1 & 8 & 9 \end{vmatrix}$$
, then find A'

Solution: Change items in rows into columns

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$$A' = \begin{vmatrix} 2 & 1 \\ 3 & 8 \\ 4 & 9 \end{vmatrix}$$
 Answer

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- Properties of Transpose of Matrix:
- 1. Transpose of transpose of a matrix is original matrix.

i.e.
$$(A')' = A$$

2. Transpose of sum of matrices is the sum of the transpose of the individual matrices.

i.e.
$$(A + B)' = A' + B'$$

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- 3. Transpose of a product of matrices is the product of the transposes of the matrices taken in reverse order.
- i.e. (AB)' = (B'A')

